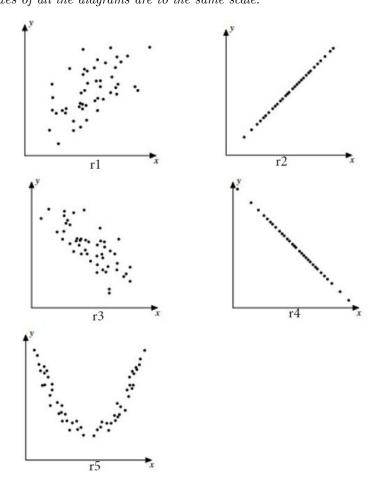
Exercise 1 \_\_\_\_\_ Calc. : X

Arrange, by increasing order of size, the linear correlation coefficients, r1, r2, r3, r4, and r5, seen in these scatter diagrams.

Give reasons for the order you have identified.

Note that the axes of all the diagrams are to the same scale.



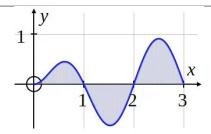
Exercise 2 Calc. : X

In a group of 500 pupils, 200 belong to the chess club, 240 to the reading club and 80 to both clubs.

Calculate the probability that a pupil chosen at random does not belong to the chess club, given that they do not belong to the reading club.

5 marks

A new company logo is shown on the right and will be made out of steel to be displayed outside the headquarters. The curve is defined by the function y = f(x).



a) **Identify** which two of the following integrals would correctly calculate the area of steel required.



1. 
$$\int_0^1 f(x) \, \mathrm{d}x + \int_1^2 f(x) \, \mathrm{d}x + \int_2^3 f(x) \, \mathrm{d}x$$

$$2. \int_0^3 f(x) \, \mathrm{d}x$$

$$3. \int_0^3 |f(x)| \, \mathrm{d}x$$

4. 
$$\int_0^1 f(x) \, dx - \int_1^2 f(x) \, dx + \int_2^3 f(x) \, dx$$

b) Explain why the other integrals would give an incorrect answer.

 $2.5 \, \mathrm{marks}$ 

Calc.: X

Exercise 4

At the start of 2022 a company bought a machine for 100 000 to make plastic items.

Each year the machine loses 20% of its value.

a) **Show** that a possible formula to model the value after x years is

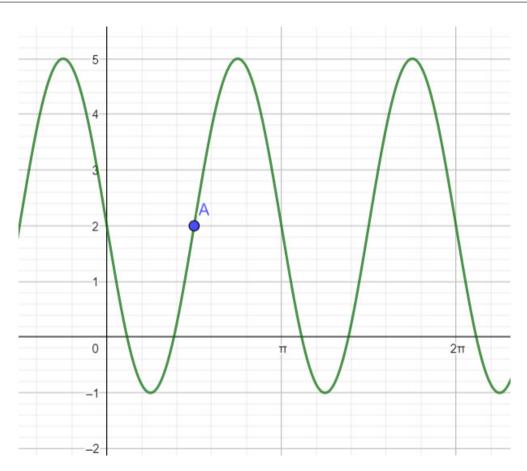
3 marks

$$P(x) = 100\ 000 \cdot e^{\ln(0.8) \cdot x}$$

b) Calculate the value of the machine at the start of 2024.

2 marks

Exercise 5 Calc.: X



The graph shown above is of a sine function, f(x), defined by:

$$f(x) = a\sin(b(x-c)) + d$$

Based on the information in the graph:

- a) **Find** the period P and **hence** the value of b.
- b) **Find** the amplitude of the function and **hence** the value of a.
- c) State the coordinates of the point A and hence find the values of c and d.

Exercise 6	Calc.: 🗶
Given $f(x) = -x^2 + 2x + 3$ :	

- a) **Find** an expression for the derivative f'(x).
- b) Find an equation for the tangent to the graph of y = f(x) at the point where x = 2.

Exercise 7 Calc.: X The height of a tree in cm is given by the function h(t), where t is the number of weeks since it was planted. Give an interpretation concerning the growth of the tree for each of the following:

- a) h(3) = 80.
- b) h'(2) = 4.
- c) The value of t when h'(t) = 0.

1.5 marks

1.5 marks

 $2~\mathrm{marks}$ 

2.5 marks

 $2.5 \,\,\mathrm{marks}$ 

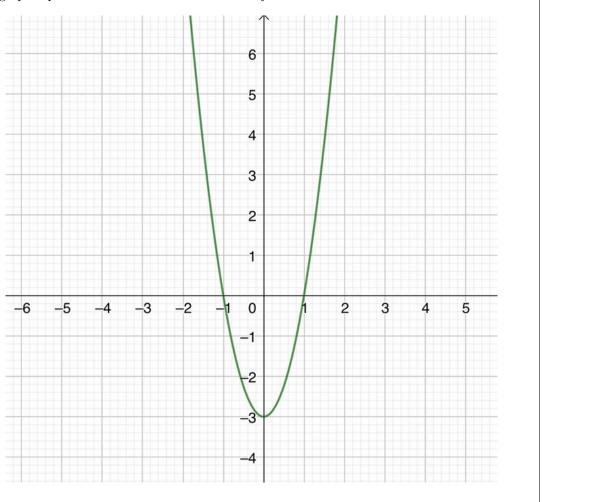
2 marks

1.5 marks

1.5 marks

Exercise 8 Calc. : X

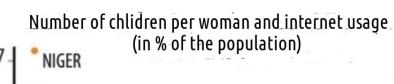
Exercise 8 The graph represents the derivative of a function f

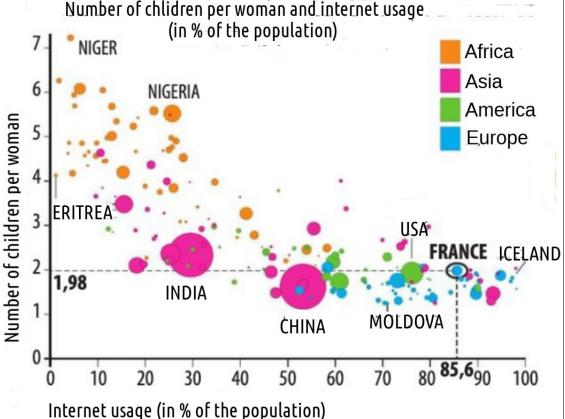


- a) **Determine** how the sign of the derivative depends on the value of x.
- b) Hence describe how the graph of function f varies in gradient.

 $2.5 \,\,\mathrm{marks}$ 

2.5 marks





a) State the variables of this graph.

1 mark

b) Identify the way in which the variables are correlated in the graph.

2 marks

c) Explain any causality that there might be between the variables.

2 marks

Exercise 10

A statistical study of two numerical variables produces the scatter diagram on the right.

- a) Show by calculation that the coordinates of the mean point are (4,6).
- $y = \frac{5}{4}x + 1$  is chosen as a regression line for the data.
- b) Show by calculation that the mean point lies on this
- c) Calculate the value of y corresponding to x = 2.
- d) We can establish from the line that a value of y = 38.5corresponds to a value of x = 30.

Comment on the whether such an extrapolation is reasonable.

