**Mathematics S7MA3**

**Part B: Examination with technological tool**

Date: Tuesday 31st January 2023

Duration: 2 hours (120 minutes)

Course: S7-MA3 EN

Teacher: K. Osborne

**Authorised material:**

- Formula booklet

- Calculator: Numworks or an alternative calculator, allowed by the school

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*Exam with* *calculator*

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| **Question B1** | **Page 1 of 3** | **Marks**  **(Total:25)** |
| ***Ski Jump***  *Part 1 (Parts 1, 2 and 3 of this question can be solved independently.)*  The ramp of a ski jump is shown in the diagram below and can be modelled by the function .  f(x)  A  The function is defined in the interval shown in the diagram with the equation:    , where and are expressed in meters.   1. Use the equation and the information in the graph to **determine** the domain of . 2. **Calculate** the area A. 3. When a skier is at the end of the ramp, the skis define a tangent line to the graph of **Define** this tangent line and show every step in your calculation. 4. The skier is at the lowest point on the ski ramp. **Calculate** the height at the lowest point on the ski ramp. **Explain** your method. | | 2  3  4  4 |

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| **Question B1** | **Page 2 of 3** | **Marks** |
| *Part 2*  *Use the following definitions for Parts 2 and 3:*   * *The position of an object is determined by the function where t is the time in seconds and s is expressed in meters.* * *The velocity function is defined as .* * *The acceleration function is defined as .*   After taking off from the ramp, the skier flies through the air until he lands on the ground. The time time between take-off and landing is exactly 3 seconds. The velocity function (in ) of the flying skier is shown in the graph below (with in seconds).  U:\Courses 2022-2023\S7 Maths 3\geogebra-export (1).png   1. **Find** the velocity *(in*  of the skier when he lands on the ground. 2. Use the available information in the diagram to **calculate** an approximation for the area A. **Explain** your method. 3. Is the approximation for the area A from question f ) an *underestimation* or an *overestimation* of the exact area? **Justify** your answer. 4. **Interpret** what the exact area A means in the given context. | | 1  3  2  2 |

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| **Question B1** | **Page 3 of 3** | **Marks** |
| *Part 3*  As the skier lands on the landing slope, he slows down until he comes to a complete stop. The velocity of the skier on the landing slope can be modelled by the function:    where is in seconds and corresponds to the moment when the skis touch the ground.   1. How long does it take for the skier to slow down to a complete stop? **Justify** your answer. 2. **Investigate** whether a landing slope of 120 m is long enough for the skier. | | 2  2 |

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| **Question B2** | **Page 1 of 2** | **Marks**  **(Total: 25)** |
| **The Island**  Part 1 *(Parts 1 and 2 of this question can be solved independently.)*  The table below gives the measured population on an island.   |  |  |  | | --- | --- | --- | | ***Beginning of the year*** | 2015 | 2020 | | ***Population*** | 5500 | 7250 |  1. Use a *linear model* to ***predict*** the population at the beginning of 2023. 2. Peter uses an *exponential model* to model the population. In this model corresponds to the beginning of 2015 and and are parameters. **Find** the parameters and of the model . 3. **Show** that the exponential model adequately fits the given data.   For questions d), e) and f), you can use the exponential model  In this model corresponds to the beginning of 2015.   1. **Determine** the annual growth rate of the exponential model. 2. **Calculate** and **interpret** what the result means in the given context. 3. Use the exponential model to **find** in which year the population would reach 10000 people.   At the beginning of 2022, the island was hit by an earthquake. Although nobody was hurt in the event, 6000 people decided to leave the island immediately. After they left, the growth rate of the island population was the same as before.   1. **Investigate** in which year the island population will be the same as it was at the beginning of 2015. | | 2  3  2  2  2  3  3 |

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| **Question B2** | **Page 2 of 2** | **Marks** |
| Part 2  *The day length* is the time between sunrise and sunset. Peter lives on the island and measured the day length of every first day of the month during a whole (non-leap) year. The results are given below:   |  |  |  |  |  |  |  | | --- | --- | --- | --- | --- | --- | --- | | ***Date*** | 1st of Jan | 1st of Feb | 1st of Mar | 1st of Apr | 1st of May | 1st of Jun | | ***Daylength (in hours)*** | 7.67 | 8.55 | 10 | 11.2 | 12.33 | 13 |  |  |  |  |  |  |  |  | | --- | --- | --- | --- | --- | --- | --- | | ***Date*** | 1st of Jul | 1st of Aug | 1st of Sep | 1st of Oct | 1st of Nov | 1st of Dec | | ***Daylength (in hours)*** | 13.05 | 12.67 | 11.6 | 10.35 | 8.95 | 7.83 |   Peter models the day length with the periodic model  , where is expressed in hours, is expressed in days and corresponds to the 1st of January.   1. **Explain** why the day length can be modelled with a periodic model and **give** the period of this model. 2. **Estimate** the amplitude of this periodic model. 3. Hence, **investigate** for which values of the parameters and the periodic model fits the data adequately. | | 2  2  4 |