## The Pythagorean Theorem I



## The Pythagorean Theorem II



Behold!

The Pythagorean Theorem III


## The Pythagorean Theorem IV



The Pythagorean Theorem V

-James A. Garfield (1876)
$20^{\text {th }}$ President of the United States

The Pythagorean Theorem VI


## The Pythagorean Theorem VII


—Annairizi of Arabia (circa A.D. 900)

## The Pythagorean Theorem VIII



The Pythagorean Theorem IX


## The Pythagorean Theorem X



-J. E. Böttcher

## The Pythagorean Theorem XI



## The Pythagorean Theorem XII



## The Pythagorean Theorem XIII


$a$

$b$

-José A. Gomez

## The Pythagorean Theorem XIV



$$
a^{2}+b^{2}=c^{2} .
$$

## The Pythagorean Theorem XV



$$
\begin{aligned}
(2 c)^{2} & =2 c^{2}+2 a^{2}+2 b^{2} \\
\therefore c^{2} & =a^{2}+b^{2} .
\end{aligned}
$$

## The Pythagorean Theorem XVI

The Pythagorean theorem (Proposition I. 47 in Euclid's Elements) is usually illustrated with squares drawn on the sides of a right triangle. However, as a consequence of Proposition VI. 31 in the Elements, any set of three similar figures may be used, such as equilateral triangles as shown at the right. Let $T$ denote the area of a right triangle with legs $a$ and $b$ and hypotenuse $c$, let $T_{a}, T_{b}$, and $T_{c}$ denote the areas of equilateral triangles drawn externally on sides $a, b$, and $c$, and let $P$ denote the area of a parallelogram with sides $a$ and $b$ and $30^{\circ}$ and $150^{\circ}$ angles. Then we have


1. $T=P$.

Proof.

2. $T_{c}=T_{a}+T_{b}$.

Proof.


